

Graduate IO: Session 1

September 12, 2016

Agenda

- ▶ course overview

Agenda

- ▶ course overview
- ▶ brief Introduction to IO

Agenda

- ▶ course overview
- ▶ brief Introduction to IO
- ▶ “New Empirical IO” (NEIO) approach: Genesove and Mullin (1998)

Agenda

- ▶ course overview
- ▶ brief Introduction to IO
- ▶ “New Empirical IO” (NEIO) approach: Genesove and Mullin (1998)
- ▶ Oligopoly Pricing in Homogenous Products Markets

Course Description and Prerequisites

- ▶ graduate level introduction to IO
 - ▶ economic theory
 - ▶ industry and data
 - ▶ econometric tools
 - ▶ computational methods

Course Description and Prerequisites

- ▶ graduate level introduction to IO
 - ▶ economic theory
 - ▶ industry and data
 - ▶ econometric tools
 - ▶ computational methods

- ▶ prerequisites
 - ▶ advanced microeconomics and econometrics
 - ▶ coding skills in Stata and Matlab
 - ▶ (not required) research experience in some industries

Topics

- ▶ essential topics in IO
 1. static models of oligopolistic competition
 2. product differentiation
 3. price discrimination
 4. market structure and entry

Topics

- ▶ essential topics in IO
 1. static models of oligopolistic competition
 2. product differentiation
 3. price discrimination
 4. market structure and entry

- ▶ areas of active research
 1. price dispersion and consumer search
 2. advertising
 3. vertical contracts and integration

Assignments

- ▶ attendance and ongoing readings: 15%
 - ▶ assign one or two readings at the end of each session
 - ▶ randomly call someone about the readings in the next session
 - ▶ 3-5 minutes: clearly state the research question and explain the strategy for answering it

Assignments

- ▶ attendance and ongoing readings: 15%
 - ▶ assign one or two readings at the end of each session
 - ▶ randomly call someone about the readings in the next session
 - ▶ 3-5 minutes: clearly state the research question and explain the strategy for answering it
- ▶ two problem sets: 30%
 - ▶ micro theory: math derivation
 - ▶ empirical: programming in Stata/Matlab

Assignments

- ▶ attendance and ongoing readings: 15%
 - ▶ assign one or two readings at the end of each session
 - ▶ randomly call someone about the readings in the next session
 - ▶ 3-5 minutes: clearly state the research question and explain the strategy for answering it
- ▶ two problem sets: 30%
 - ▶ micro theory: math derivation
 - ▶ empirical: programming in Stata/Matlab
- ▶ one assigned paper: 55%
 - ▶ 45 minutes group presentation: 35%
 - ▶ referee report: 20%

Expectations

- ▶ goal: transition from being consumers of research to being producers of research
 - ▶ how to: read other people's papers, evaluate your own ideas for papers, do practical stuff (e.g., coding in Stata/Matlab), construct a complete research paper

Expectations

- ▶ goal: transition from being consumers of research to being producers of research
 - ▶ how to: read other people's papers, evaluate your own ideas for papers, do practical stuff (e.g., coding in Stata/Matlab), construct a complete research paper
- ▶ in particular
 - ▶ read papers carefully before coming to class
 - ▶ participate in class discussion with comments, questions, etc.
 - ▶ complete assignment carefully and on time

IO Overview: Einav and Levin (2010)

- ▶ what is IO about?
 - ▶ structure of industries in the economy
 - ▶ behaviour of firms and individuals in these industries
 - ▶ depart from perfect competition: scale economies, market frictions, strategic behavior, etc.
 - ▶ how competition plays out in different markets and how it relates to industry structure, regulation/ public policy, etc

IO Overview: Einav and Levin (2010)

- ▶ what is IO about?
 - ▶ structure of industries in the economy
 - ▶ behaviour of firms and individuals in these industries
 - ▶ depart from perfect competition: scale economies, market frictions, strategic behavior, etc.
 - ▶ how competition plays out in different markets and how it relates to industry structure, regulation/ public policy, etc
- ▶ a brief history (since 1970s)
 - ▶ theoretical models of imperfect competition: game theory revolution (Tirole 1988)
 - ▶ empirical perspective: shift from “structure-conduct-performance” (back to Bain 1951) to “New Empirical IO” (Bresnahan 1989)

Structure-Conduct-Performance Paradigm

- ▶ cross-industry regression:

$$\text{profit}_i = \beta \times \text{concentration}_i + \text{other stuff}_i + \varepsilon_i$$

Structure-Conduct-Performance Paradigm

- ▶ cross-industry regression:

$$\text{profit}_i = \beta \times \text{concentration}_i + \text{other stuff}_i + \varepsilon_i$$

- ▶ basic assumptions
 - ▶ economic price-cost margins (profit or performance) could be directly observed in accounting data
 - ▶ cross-industry variation in industry structure could be captured by a small number of observable measures

Structure-Conduct-Performance Paradigm

- ▶ cross-industry regression:

$$\text{profit}_i = \beta \times \text{concentration}_i + \text{other stuff}_i + \varepsilon_i$$

- ▶ basic assumptions
 - ▶ economic price-cost margins (profit or performance) could be directly observed in accounting data
 - ▶ cross-industry variation in industry structure could be captured by a small number of observable measures
- ▶ what were the results?
 - ▶ often $\beta_1 > 0$: more concentrated industries are more profitable
 - ▶ so what? is this causal? not really, because hard to find *exogeneous* variation to shift concentration
 - ▶ what are the policy prescriptions? reduce concentration to lower price?

New Empirical IO (NEIO) Paradigm

- ▶ key features:
 - ▶ individual industries are taken to have important idiosyncracies: focus on a single industry/market
 - ▶ firms' price-cost margins are not taken to be observables: economic marginal cost cannot be directly observed, but infered from firm behavior

New Empirical IO (NEIO) Paradigm

- ▶ key features:
 - ▶ individual industries are taken to have important idiosyncracies: focus on a single industry/market
 - ▶ firms' price-cost margins are not taken to be observables: economic marginal cost cannot be directly observed, but inferred from firm behavior
- ▶ advantages
 - ▶ detailed micro data and institutional knowledge
 - ▶ clarity of economic theory
 - ▶ convincing empirical measurement/econometric identification
 - ▶ counterfactual analysis: what would happen following a merger or regulatory change

Genesove and Mullin (1998)

- ▶ in the NEIO literature, equilibrium oligopoly price P is characterized by the generalized monopolist's first-order condition

$$P + \theta QP'(Q) = mc \quad (1)$$

where Q is industry output, θ is the conduct or market power parameter, mc is the marginal cost

Genesove and Mullin (1998)

- ▶ in the NEIO literature, equilibrium oligopoly price P is characterized by the generalized monopolist's first-order condition

$$P + \theta QP'(Q) = mc \quad (1)$$

where Q is industry output, θ is the conduct or market power parameter, mc is the marginal cost

- ▶ the parameter θ is called “the average collusiveness of conduct” (Bresnahan 1989)
 - ▶ perfect collusion or monopoly: $\theta = 1$
 - ▶ perfect competition or Bertrand: $\theta = 0$
 - ▶ symmetric Cournot: $\theta = \frac{1}{N}$, where N is the number of firms in the industry

Genesove and Mullin (1998)

- ▶ in the NEIO literature, equilibrium oligopoly price P is characterized by the generalized monopolist's first-order condition

$$P + \theta QP'(Q) = mc \quad (1)$$

where Q is industry output, θ is the conduct or market power parameter, mc is the marginal cost

- ▶ the parameter θ is called “the average collusiveness of conduct” (Bresnahan 1989)
 - ▶ perfect collusion or monopoly: $\theta = 1$
 - ▶ perfect competition or Bertrand: $\theta = 0$
 - ▶ symmetric Cournot: $\theta = \frac{1}{N}$, where N is the number of firms in the industry
- ▶ two major uses of (1)
 - ▶ estimate θ as a free parameter, along with cost parameters, using data on a sample of markets
 - ▶ prior choice of θ is assumed, so marginal cost can be directly inferred

Motivation of This Paper

- ▶ typically impose strong functional-form assumptions on demand: misspecifications might lead to incorrect inference about market power or marginal cost

Motivation of This Paper

- ▶ typically impose strong functional-form assumptions on demand: misspecifications might lead to incorrect inference about market power or marginal cost
- ▶ the NEIO approach has never been “tested”: requires that one have alternative measures of conduct and cost with which the NEIO estimates could be compared

Motivation of This Paper

- ▶ typically impose strong functional-form assumptions on demand: misspecifications might lead to incorrect inference about market power or marginal cost
- ▶ the NEIO approach has never been “tested”: requires that one have alternative measures of conduct and cost with which the NEIO estimates could be compared
- ▶ this paper: assesses the NEIO approach, using US East Coast cane sugar refining industry, 1890-1941
 - ▶ production technology is simple: raw sugar is transformed to refined sugar, at a fixed and known coefficient
 - ▶ the industry underwent dramatic changes in the degree of competition

Industry Background

- ▶ refined sugar: homogeneous product, prices tended toward uniformity

Industry Background

- ▶ refined sugar: homogeneous product, prices tended toward uniformity
- ▶ geographic market: cane sugar refining on East Coast of US, basis price determined in New York City

Industry Background

- ▶ refined sugar: homogeneous product, prices tended toward uniformity
- ▶ geographic market: cane sugar refining on East Coast of US, basis price determined in New York City
- ▶ fringe suppliers of refined sugar: domestic and European beet sugar producers; not much of a threat for most of the sample period, so not incorporated in the analysis

Industry Background

- ▶ early history:
 - ▶ American Sugar Refining Company (ASRC), formed in 1887 as a consolidation of 18 firms controlling 80% of the industry's capacity
 - ▶ the firms quickly reorganized and reduced to 10, refined prices rose 16%
 - ▶ a major entry (plant construction) happened in 1889, which led to a price war
 - ▶ then an acquisition campaign lunched by ASRC raised its share of capacity to 95% by 1892

Industry Background

- ▶ early history:
 - ▶ American Sugar Refining Company (ASRC), formed in 1887 as a consolidation of 18 firms controlling 80% of the industry's capacity
 - ▶ the firms quickly reorganized and reduced to 10, refined prices rose 16%
 - ▶ a major entry (plant construction) happened in 1889, which led to a price war
 - ▶ then an acquisition campaign launched by ASRC raised its share of capacity to 95% by 1892

- ▶ basic pattern: high concentration → firms entry and price wars → acquisition by ASRC

Industry Background

- ▶ early history:
 - ▶ American Sugar Refining Company (ASRC), formed in 1887 as a consolidation of 18 firms controlling 80% of the industry's capacity
 - ▶ the firms quickly reorganized and reduced to 10, refined prices rose 16%
 - ▶ a major entry (plant construction) happened in 1889, which led to a price war
 - ▶ then an acquisition campaign launched by ASRC raised its share of capacity to 95% by 1892
- ▶ basic pattern: high concentration → firms entry and price wars → acquisition by ASRC
- ▶ entry eroded ASRC's capacity share between 1892 and 1900, precipitating a price war that ended in consolidation, cartel from 1900-11, followed by an anti-trust investigation

Cost Structure

- ▶ technology is simple and common to all the firms: marginal cost can be summarized by

$$MC = c_0 + k \times P_{\text{raw}}$$

- ▶ MC : the marginal cost of producing 100 lbs of refined sugar
- ▶ c_0 : variable cost: \$0.26 for producing 100 lbs of refined sugar
- ▶ k : conversion ratio: 1.041 (1 lb of raw sugar = .96 lb of refined sugar)
- ▶ P_{raw} : price of 100 lbs of raw sugar

Cost Structure

- ▶ technology is simple and common to all the firms: marginal cost can be summarized by

$$MC = c_0 + k \times P_{\text{raw}}$$

- ▶ MC : the marginal cost of producing 100 lbs of refined sugar
 - ▶ c_0 : variable cost: \$0.26 for producing 100 lbs of refined sugar
 - ▶ k : conversion ratio: 1.041 (1 lb of raw sugar = .96 lb of refined sugar)
 - ▶ P_{raw} : price of 100 lbs of raw sugar
-
- ▶ entry costs are substantial: mostly plant and machinery cost which are sunk - no resale value

Cost Structure

- ▶ technology is simple and common to all the firms: marginal cost can be summarized by

$$MC = c_0 + k \times P_{\text{raw}}$$

- ▶ MC : the marginal cost of producing 100 lbs of refined sugar
 - ▶ c_0 : variable cost: \$0.26 for producing 100 lbs of refined sugar
 - ▶ k : conversion ratio: 1.041 (1 lb of raw sugar = .96 lb of refined sugar)
 - ▶ P_{raw} : price of 100 lbs of raw sugar
-
- ▶ entry costs are substantial: mostly plant and machinery cost which are sunk - no resale value
-
- ▶ ASRC retained substantial excess capacity for entire sample period

Demand Model

- ▶ a simple linear demand model

$$Q(P) = \beta(\alpha - P) + \epsilon$$

- ▶ P : quarterly price of 100 lbs. of refined sugar
- ▶ β : measure of size of market
- ▶ α : maximum willingness to pay
- ▶ ϵ : unobserved demand shock

Demand Model

- ▶ a simple linear demand model

$$Q(P) = \beta(\alpha - P) + \epsilon$$

- ▶ P : quarterly price of 100 lbs. of refined sugar
 - ▶ β : measure of size of market
 - ▶ α : maximum willingness to pay
 - ▶ ϵ : unobserved demand shock
-
- ▶ sugar is an input into fruit canning which occurs in the third quarter: demand parameters can differ in high season from other quarters (basically two demand curves)

$$Q(P) = \begin{cases} \beta_H(\alpha_H - P) + \epsilon & \text{high season} \\ \beta_L(\alpha_L - P) + \epsilon & \text{low season} \end{cases}$$

Endogeneity Problem

- ▶ OLS gives biased estimates of β since P is endogenous: high demand shocks will raise price

Endogeneity Problem

- ▶ OLS gives biased estimates of β since P is endogenous: high demand shocks will raise price
- ▶ need to find a variable that is correlated with P but not with demand shock (known as an instrument)

Endogeneity Problem

- ▶ OLS gives biased estimates of β since P is endogenous: high demand shocks will raise price
- ▶ need to find a variable that is correlated with P but not with demand shock (known as an instrument)
- ▶ usually use input prices that shift supply: helps determine P but typically independent of demand shocks

Instrument

- ▶ the “natural” instrument is P_{raw} , but
 - ▶ P_{raw} is probably not exogenous because US consumption is 25% of world market: likely to be correlated with US demand shocks

Instrument

- ▶ the “natural” instrument is P_{raw} , but
 - ▶ P_{raw} is probably not exogenous because US consumption is 25% of world market: likely to be correlated with US demand shocks
- ▶ Cuban imports as an instrument: a proxy for Cuban production of raw sugar
 - ▶ Cuban raw sugar represents a substantial share of total U.S. imports of raw sugar: variation in Cuban imports affects price of raw sugar and hence price of refined sugar
 - ▶ but variation in Cuban imports is due to supply factors such as weather: independent of U.S. demand shocks
 - ▶ bottom line: regardless of the level of production, almost always 100% of Cuban production were shipped to US, during the sample period

Demand Estimates

TABLE 3 Demand for Refined Sugar, Separately by Season

	(1) Quadratic ($\gamma = 2$)	(2) Linear ($\gamma = 1$)	(3) Log-Linear ($\alpha = 0$)	(4) Exponential ($\gamma, \alpha \rightarrow \infty$)
Low season [N = 73]				
<i>Refined Price</i>	α_L 7.72 (.86)	β_L -2.30 (.48)	γ_L -2.03 (.48)	$\left(\frac{\gamma}{\alpha}\right)_L$ -.53 (.12)
Intercept	-1.20 (.47)	$\beta\alpha_L$ 13.37 (1.90)	4.19 (.65)	3.52 (.48)
High season [N = 24]				
<i>Refined Price</i>	α_H 11.88 (2.03)	β_H -1.36 (.36)	γ_H -1.10 (.28)	$\left(\frac{\gamma}{\alpha}\right)_H$ -.26 (.07)
Intercept	-2.48 (.54)	$\beta\alpha_H$ 10.74 (1.57)	3.17 (.40)	2.70 (.29)
$\chi^2_{(2)}$ test	6.90	28.18	29.17	25.96

Notes: Standard errors are in parentheses. They are heteroskedasticity-robust and corrected for serial correlation with four lags, by the method of Newey and West (1987). *Refined Price* is instrumented by the log of *Cuban Imports*. The reported $\chi^2_{(2)}$ statistic is for the joint test of equality of the coefficients on price and the intercept across seasons.

- ▶ demand is larger and less elastic in high season

"Guessing" the Conduct Parameter

TABLE 2 **Sample Statistics**

	Full Sample		Low Season		High Season	
	Mean	Standard Deviation	Mean	Standard Deviation	Mean	Standard Deviation
<i>Refined Price (P)</i>	4.03	.62	3.99	.63	4.14	.58
<i>Raw Price (P_{RAW})</i>	3.30	.59	3.28	.61	3.36	.53

- ▶ price is only slightly higher in high season: the market power is quite weak
- ▶ thus, θ should be small, though positive

Pricing Rule

- ▶ basic markup equation

$$\frac{P - MC}{P} = \frac{\theta}{\eta(P)}$$

- ▶ LHS is known as the Lerner index
- ▶ θ is “the average collusiveness of conduct” (Bresnahan 1989)
- ▶ special cases: $\theta = 1$ if monopoly; $\theta = 0$ if competitive; $\theta = s_i$ if Cournot

Pricing Rule

- ▶ basic markup equation

$$\frac{P - MC}{P} = \frac{\theta}{\eta(P)}$$

- ▶ LHS is known as the Lerner index
 - ▶ θ is “the average collusiveness of conduct” (Bresnahan 1989)
 - ▶ special cases: $\theta = 1$ if monopoly; $\theta = 0$ if competitive; $\theta = s_i$ if Cournot
- ▶ in this case, $\eta(P) = P / (\alpha - P)$, so pricing rule is

$$P = \frac{\theta\alpha + c_0 + kP_{\text{raw}}}{1 + \theta}$$

Estimation

- ▶ suppose P_{raw} is exogenous, we could run this regression

$$P = \beta_0 + \beta_1 \times 1(\text{high season}) + \beta_2 \times P_{\text{raw}}$$

- ▶ then use $(\beta_0, \beta_1, \beta_2)$ and (α_L, α_H) to recover (θ, c_0, k)

Estimation

- ▶ suppose P_{raw} is exogenous, we could run this regression

$$P = \beta_0 + \beta_1 \times 1(\text{high season}) + \beta_2 \times P_{\text{raw}}$$

- ▶ then use $(\beta_0, \beta_1, \beta_2)$ and (α_L, α_H) to recover (θ, c_0, k)
- ▶ P_{raw} is endogenous and but we can use the moment condition restriction

$$E[\{P(1 + \theta) - \theta\alpha - c_0 - kP_{\text{raw}}\}Z] = 0$$

- ▶ instruments:
 $Z = (\text{constant}, 1(\text{high season}), \log(\text{Cuban Imports}))$

Results

TABLE 7 NLIV Estimates of Pricing Rule Parameters

	Linear		Direct Measure
	(1)	(2)	(3)
$\hat{\theta}$.038 (.024)	.037 (.024)	.10
\hat{c}_o	.466 (.285)	.39 (.061)	.26
\hat{k}	1.052 (.085)		1.075

- ▶ market is a lot more competitive than monopoly or even Cournot (with nine firms or fewer firms)
- ▶ the NEIO approach performs reasonably well although variable cost is overestimated
- ▶ column (2) imposes the value of k : does not improve the estimate of θ , but raises the precision

Summary of NEIO Approach

- ▶ firms' price-cost margins are not taken to be observables: marginal cost is inferred from firm behavior (i.e., FOC)

Summary of NEIO Approach

- ▶ firms' price-cost margins are not taken to be observables: marginal cost is inferred from firm behavior (i.e., FOC)
- ▶ individual industries have important idiosyncracies: firm's conduct is likely to vary across industries based on these unobserved industry-specific factors so little can be learned from cross-sectional studies of industries

Summary of NEIO Approach

- ▶ firms' price-cost margins are not taken to be observables: marginal cost is inferred from firm behavior (i.e., FOC)
- ▶ individual industries have important idiosyncracies: firm's conduct is likely to vary across industries based on these unobserved industry-specific factors so little can be learned from cross-sectional studies of industries
- ▶ the behavioral equations by which firms set prices and quantities are estimated and the structural parameters identified

Oligopoly Pricing in Homogenous Products Markets

- ▶ main question: how are prices and output determined when there are a small number of firms producing a homogenous (identical) product?

Oligopoly Pricing in Homogenous Products Markets

- ▶ main question: how are prices and output determined when there are a small number of firms producing a homogenous (identical) product?
- ▶ monopoly models: agent optimizes against a fixed environment

Oligopoly Pricing in Homogenous Products Markets

- ▶ main question: how are prices and output determined when there are a small number of firms producing a homogenous (identical) product?
- ▶ monopoly models: agent optimizes against a fixed environment
- ▶ oligopoly models: agent has to consider what actions its competitors will take (i.e., beliefs) and how they may react to its actions (i.e., dynamics)

Oligopoly Pricing in Homogenous Products Markets

- ▶ main question: how are prices and output determined when there are a small number of firms producing a homogenous (identical) product?
- ▶ monopoly models: agent optimizes against a fixed environment
- ▶ oligopoly models: agent has to consider what actions its competitors will take (i.e., beliefs) and how they may react to its actions (i.e., dynamics)
- ▶ focus initially on static models: they will give us some insights into more complicated dynamic models

Cournot Model

- ▶ normal form representation
 - ▶ player: $i = 1, 2, \dots, N$
 - ▶ strategy for firm i : $q_i \in [0, \infty)$
 - ▶ payoff: $\pi(q_i, q_{-i}) = P(\sum_i q_i) q_i - C(q_i)$

Cournot Model

- ▶ normal form representation
 - ▶ player: $i = 1, 2, \dots, N$
 - ▶ strategy for firm i : $q_i \in [0, \infty)$
 - ▶ payoff: $\pi(q_i, q_{-i}) = P(\sum_j q_j) q_i - C(q_i)$
- ▶ interpretation: two firms decide simultaneously what quantity to produce and supply to the market, price adjusts so as to clear the market

Cournot Model

- ▶ normal form representation
 - ▶ player: $i = 1, 2, \dots, N$
 - ▶ strategy for firm i : $q_i \in [0, \infty)$
 - ▶ payoff: $\pi(q_i, q_{-i}) = P(\sum_j q_j) q_i - C(q_i)$
- ▶ interpretation: two firms decide simultaneously what quantity to produce and supply to the market, price adjusts so as to clear the market
- ▶ examples: commodity markets (e.g., spring water, sugar)

Solution Concept: Nash Equilibrium

- ▶ each firm chooses output optimally given other firms' output choices

Solution Concept: Nash Equilibrium

- ▶ each firm chooses output optimally given other firms' output choices
- ▶ formally, a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$\pi(q_i^*, q_{-i}^*) \geq \pi(q_i, q_{-i}^*) \quad \forall q_i \in [0, \infty) \quad i = 1, \dots, N$$

Solution Concept: Nash Equilibrium

- ▶ each firm chooses output optimally given other firms' output choices
- ▶ formally, a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$\pi(q_i^*, q_{-i}^*) \geq \pi(q_i, q_{-i}^*) \quad \forall q_i \in [0, \infty) \quad i = 1, \dots, N$$

- ▶ interpretation: each firm is behaving optimally given its conjecture about its rival's choice of quantity and, in equilibrium, their conjectures are correct

Solution Concept: Nash Equilibrium

- ▶ each firm chooses output optimally given other firms' output choices
- ▶ formally, a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$\pi(q_i^*, q_{-i}^*) \geq \pi(q_i, q_{-i}^*) \quad \forall q_i \in [0, \infty) \quad i = 1, \dots, N$$

- ▶ interpretation: each firm is behaving optimally given its conjecture about its rival's choice of quantity and, in equilibrium, their conjectures are correct
- ▶ problem: not very useful, typically not the case in reality

Alternative Formulation: Best-Reply Response

- ▶ let $R_i(q_{-i})$ denote firm i 's best replies to its rivals' output choices, then a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$q_i^* \in R_i(q_{-i}^*) \text{ for } i = 1, \dots, N$$

Alternative Formulation: Best-Reply Response

- ▶ let $R_i(q_{-i})$ denote firm i 's best replies to its rivals' output choices, then a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$q_i^* \in R_i(q_{-i}^*) \text{ for } i = 1, \dots, N$$

- ▶ in other words, the Nash equilibrium is a fixed point of the mapping \mathbf{R} , where \mathbf{R} is the Cartesian product of R_i

Alternative Formulation: Best-Reply Response

- ▶ let $R_i(q_{-i})$ denote firm i 's best replies to its rivals' output choices, then a Nash equilibrium is a profile $\{q_1^*, \dots, q_N^*\}$ such that

$$q_i^* \in R_i(q_{-i}^*) \text{ for } i = 1, \dots, N$$

- ▶ in other words, the Nash equilibrium is a fixed point of the mapping \mathbf{R} , where \mathbf{R} is the Cartesian product of R_i
- ▶ existence reduces to checking that \mathbf{R} meets conditions of some fixed point theorem, this also provides algorithm for finding Nash equilibria

Symmetric Case with Linear Demand

- ▶ demand: $P(Q) = a - bQ$, $Q = q_1 + \dots + q_N$
- ▶ supply: $C(q_i) = cq_i$, $i = 1, \dots, N$

Symmetric Case with Linear Demand

- ▶ demand: $P(Q) = a - bQ$, $Q = q_1 + \dots + q_N$
- ▶ supply: $C(q_i) = cq_i$, $i = 1, \dots, N$
- ▶ firm i 's optimization problem: choose q_i to maximize

$$\pi(q_i, q_{-i}) = \left[a - b \left(q_i + \sum_{j \neq i} q_j \right) - c \right] q_i$$

Symmetric Case with Linear Demand

- ▶ demand: $P(Q) = a - bQ$, $Q = q_1 + \dots + q_N$
- ▶ supply: $C(q_i) = cq_i$, $i = 1, \dots, N$
- ▶ firm i 's optimization problem: choose q_i to maximize

$$\pi(q_i, q_{-i}) = \left[a - b \left(q_i + \sum_{j \neq i} q_j \right) - c \right] q_i$$

- ▶ taking first-order condition, the best reply is

$$R(q_{-i}) \equiv q_i = \frac{a - c - b \left(\sum_{j \neq i} q_j \right)}{2b}, \quad i = 1, \dots, N$$

Symmetric Case with Linear Demand

- ▶ demand: $P(Q) = a - bQ$, $Q = q_1 + \dots + q_N$
- ▶ supply: $C(q_i) = cq_i$, $i = 1, \dots, N$
- ▶ firm i 's optimization problem: choose q_i to maximize

$$\pi(q_i, q_{-i}) = \left[a - b \left(q_i + \sum_{j \neq i} q_j \right) - c \right] q_i$$

- ▶ taking first-order condition, the best reply is

$$R(q_{-i}) \equiv q_i = \frac{a - c - b \left(\sum_{j \neq i} q_j \right)}{2b}, \quad i = 1, \dots, N$$

- ▶ solve the N equations for N unknown

$$q_i^* = \frac{a - c}{b(N + 1)}$$

Asymmetric Case

- ▶ 2 firms with marginal costs $c_1 < c_2$

Asymmetric Case

- ▶ 2 firms with marginal costs $c_1 < c_2$
- ▶ best reply functions

$$R(q_j) \equiv q_i = \frac{a - c_i - bq_j}{2b}$$

Asymmetric Case

- ▶ 2 firms with marginal costs $c_1 < c_2$
- ▶ best reply functions

$$R(q_j) \equiv q_i = \frac{a - c_i - bq_j}{2b}$$

- ▶ solution (equilibrium)

$$q_i^* = \frac{a - 2c_i + c_j}{3b}$$

- ▶ interpretation: the more efficient (lower cost) firm produces more output

Markups

- ▶ evaluated at the equilibrium, the FOC can be written as

$$\frac{P(Q^*) - c_i}{P(Q^*)} = \frac{s_i^*}{\eta^*}$$

where $s_i^* = \frac{q_i^*}{Q^*}$ is firm i 's market share and η^* is the the elasticity of market demand

Markups

- ▶ evaluated at the equilibrium, the FOC can be written as

$$\frac{P(Q^*) - c_i}{P(Q^*)} = \frac{s_i^*}{\eta^*}$$

where $s_i^* = \frac{q_i^*}{Q^*}$ is firm i 's market share and η^* is the the elasticity of market demand

- ▶ firms have market power (price is above marginal cost)
- ▶ the more elastic is demand, the lower are the markups
- ▶ firms with lower marginal costs have higher market shares
- ▶ more firms \Rightarrow smaller shares \Rightarrow lower markups
- ▶ solution lies between competition and monopoly

Bertrand Model

- ▶ price competition: simultaneously choose prices
 - ▶ firms' products are perfect substitutes: consumers buy from firm offering the lowest price

Bertrand Model

- ▶ price competition: simultaneously choose prices
 - ▶ firms' products are perfect substitutes: consumers buy from firm offering the lowest price
- ▶ players: two firms indexed by $i = 1, 2$
- ▶ strategy of firm i : $p_i \in [0, \infty)$
- ▶ payoffs

$$\pi_i(p_i, p_j) = \begin{cases} p_i D(p_i) - C(D(p_i)) & \text{if } p_i < p_j \\ \frac{1}{2} [p_i D(p_i) - C(D(p_i))] & \text{if } p_i = p_j \\ 0 & \text{if } p_i > p_j \end{cases}$$

Solution

- ▶ Nash Equilibrium: a pair of prices $\{p_1^*, p_2^*\}$ such that

$$\pi_i(p_i^*, p_j^*) \geq \pi_i(p_i, p_j^*) \quad \forall p_i \in [0, \infty) \quad i = 1, 2$$

- ▶ payoff functions are discontinuous, best-reply functions are not well-defined

Solution

- ▶ Nash Equilibrium: a pair of prices $\{p_1^*, p_2^*\}$ such that

$$\pi_i(p_i^*, p_j^*) \geq \pi_i(p_i, p_j^*) \quad \forall p_i \in [0, \infty) \quad i = 1, 2$$

- ▶ payoff functions are discontinuous, best-reply functions are not well-defined
- ▶ unique NE: $p_1^* = p_2^* = c$
 - ▶ can $p_1 > p_2 > c$ be an equilibrium?
 - ▶ can $p_1 = p_2 > c$ be an equilibrium?
 - ▶ no, because it is profitable to undercut rival

Bertrand Paradox

- ▶ one is monopoly, two is perfect competition?
 - ▶ puzzle: firms do not typically sell at marginal costs in markets with few sellers

Bertrand Paradox

- ▶ one is monopoly, two is perfect competition?
 - ▶ puzzle: firms do not typically sell at marginal costs in markets with few sellers
- ▶ price competition seems more natural than quantity competition but yields predictions that contradict reality
 - ▶ unlimited capacity: in reality firms may not have the capacity to serve the whole market
 - ▶ homogeneous good: in reality it's rare for two firms' products to be perfect substitutes
 - ▶ static competition: in reality firms play pricing games against each other repeatedly
 - ▶ perfect information: in reality consumers may have to engage in costly search to determine which firm has the lowest price

Bertrand Paradox

- ▶ one is monopoly, two is perfect competition?
 - ▶ puzzle: firms do not typically sell at marginal costs in markets with few sellers
- ▶ price competition seems more natural than quantity competition but yields predictions that contradict reality
 - ▶ unlimited capacity: in reality firms may not have the capacity to serve the whole market
 - ▶ homogeneous good: in reality it's rare for two firms' products to be perfect substitutes
 - ▶ static competition: in reality firms play pricing games against each other repeatedly
 - ▶ perfect information: in reality consumers may have to engage in costly search to determine which firm has the lowest price
- ▶ relaxing any one of these assumptions yields a richer model with more realistic predictions

Readings for Next Session

- ▶ D. Kreps and J. Scheinkman, “Quantity Precommitment and Bertrand Competition Yield Cournot Outcomes,” *Bell Journal of Economics*, 1983.